

CLAIMS

We claim:

1. An apparatus for block coding of windows of digitally represented images comprising a chain of lattices of lapped transforms with dyadic rational lifting steps.

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2. An apparatus for coding, storing or transmitting, and decoding $M \times M$ sized blocks of digitally represented images, where M is ~~a power of 2~~^{an even number}, comprising

a. a forward transform comprising

i. a base transform having M channels numbered 0 through $M-1$, half of said channel numbers being odd and half being even;

ii. an equal normalization factor in each of the M channels selected to be dyadic-rational;

iii. a full-scale butterfly implemented as a series of lifting steps with a first set of dyadic rational coefficients;

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iv. $M/2$ delay lines in the odd numbered channels;

v. a full-scale butterfly implemented as a series of lifting steps with said first set of dyadic rational coefficients; and

vi. a series of lifting steps in the odd numbered channels with a second specifically selected set of dyadic-rational coefficients;

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b. means for transmission or storage of the transform output coefficients; and

c. an inverse transform comprising

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- i. M channels numbered 0 through M-1, half of said channel numbers being odd and half being even;
- ii. a series of inverse lifting steps in the odd numbered channels with said second set of specifically selected dyadic-rational coefficients;
- iii. a full-scale butterfly implemented as a series of lifting steps with said first set of specifically selected dyadic-rational coefficients;
- iv. M/2 delay lines in the even numbered channels;
- v. a full-scale butterfly implemented as a series of lifting steps with said first set of specifically selected dyadic-rational coefficients;
- vi. an equal denormalization factor in each of the M channels specifically selected to be dyadic-rational; and
- vii. a base inverse transform having M channels numbered 0 through M-1.

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- 2. The apparatus of Claim 2 in which the normalizing factor takes the value 25/16 and simultaneously the denormalizing factor takes the value 16/25.
- 3. The apparatus of Claim 2 in which the normalizing factor takes the value 5/4 and simultaneously the denormalizing factor takes the value 4/5.
- 4. The apparatus of Claim 2 in which the first set of dyadic rational coefficients are all equal to 1.
- 5. The apparatus of Claim 2 in which the second set of dyadic rational coefficients are all equal to $\frac{1}{2}$.
- 6. The apparatus of Claim 2 in which the base transform is any $M \times M$ invertible matrix of the

form of a linear phase filter and the inverse base transform is the inverse of said $M \times M$ invertible matrix.

2. 8. The apparatus of Claim 2 in which the base transform is the forward $M \times M$ discrete cosine transform and the inverse base transform is the inverse $M \times M$ discrete cosine transform.

5 9. An apparatus for transforming $M \times M$ blocks of digital image intensities comprising lapped transforms with overlapping factor K and having butterfly structures and lifting steps to generate M -channel uniform linear phase perfect reconstruction filter banks.

10. The apparatus of Claim 9 in which K equals 2.

8. 11. An apparatus for coding, compressing, storing or transmitting, and decoding a block of $M \times M$ intensities from a digital image selected by an $M \times M$ window moving recursively over the image, comprising:

a. an $M \times M$ block transform comprising:

- i. an initial stage
- ii. a normalizing factor in each channel

15 b. a cascade comprising a plurality of dyadic rational lifting transforms, each of said plurality of dyadic rational lifting transforms comprising

- i. a first bank of pairs of butterfly lifting steps with unitary coefficients between adjacent lines of said transform;
- ii. a bank of delay lines in a first group of $M/2$ alternating lines;
- iii. a second bank of butterfly lifting steps with unitary coefficients, and

iv. a bank of pairs of butterfly lifting steps with coefficients of 1/2 between $M/2 - 1$ pairs of said $M/2$ alternating lines;

c. means for transmission or storage of the output coefficients of said $M \times M$ block transform; and

5 d. an inverse transform comprising

i. a cascade comprising a plurality of dyadic rational lifting transforms, each of said plurality of dyadic rational lifting transforms comprising

a) a bank of pairs of butterfly lifting steps with coefficients of 1/2 between said $M/2 - 1$ pairs of said $M/2$ alternating lines;

b) a first bank of pairs of butterfly lifting steps with unitary coefficients between adjacent lines of said transform;

c) a bank of delay lines in a second group of $M/2$ alternating lines; and

d) a second bank of pairs of butterfly lifting steps with unitary coefficients between adjacent lines of said transform;

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15 ii. a de-scaling bank; and

iii. an inverse initial stage.

12. A method of block coding windows of digitally represented images comprising successive steps of processing the output of each step through a following step in a chain of lattices of lapped transforms with dyadic rational lifting steps.

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13. A method of coding, storing or transmitting, and decoding $M \times M$ sized blocks of digitally represented images, where M is ~~a power of 2~~^{an even number}, comprising

- a. transmitting the original picture signals to a coder, which effects the steps of
 - 5 i. converting the signals with a base transform having M channels numbered 0 through $M-1$, half of said channel numbers being odd and half being even;
 - ii. normalizing the output of the preceding step with a dyadic rational normalization factor in each of said M channels;
 - iii. processing the output of the preceding step through two lifting steps with a first set of identical dyadic rational coefficients connecting each pair of adjacent numbered channels in a butterfly configuration;
 - iv. transmitting the resulting coefficients through $M/2$ delay lines in the odd numbered channels;
 - v. processing the output of the preceding step through two inverse lifting steps with the first set of dyadic rational coefficients connecting each pair of adjacent numbered channels in a butterfly configuration; and
 - vi. applying two lifting steps with a second set of identical dyadic rational coefficients connecting each pair of adjacent odd numbered channels to the output of the preceding step;
- 20 b. transmitting or storing the transform output coefficients;
- c. receiving the transform output coefficients in a decoder; and
- d. processing the output coefficients in a decoder, comprising the steps of

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- i. receiving the coefficients in M channels numbered 0 through $M-1$, half of said channel numbers being odd and half being even;
- ii. applying two inverse lifting steps with dyadic rational coefficients connecting each pair of adjacent odd numbered channels;
- iii. applying two lifting steps with dyadic rational coefficients connecting each pair of adjacent numbered channels in a butterfly configuration;
- iv. transmitting the result of the preceding step through $M/2$ delay lines in the even numbered channels;
- v. applying two inverse lifting steps with dyadic rational coefficients connecting each pair of adjacent numbered channels in a butterfly configuration;
- vi. denormalizing the result of the preceding step with a dyadic rational inverse normalization factor in each of said M channels; and
- vii. processing the result of the preceding step through a base inverse transform having M channels numbered 0 through $M-1$.

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15 14. A method of coding, compressing, storing or transmitting, and decoding a block of $M \times M$ intensities from a digital image selected by an $M \times M$ window moving recursively over the image, comprising the steps of:

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- a. Processing the intensities in an $M \times M$ block coder comprising the steps of:
 - i. processing the intensities through an initial stage;
 - ii. scaling the result of the preceding step in each channel;
- b. processing the result of the preceding step through a cascade comprising a plurality of

dyadic rational lifting transforms, each of said plurality of dyadic rational lifting transforms comprising

- i. a first bank of pairs of butterfly lifting steps with unitary coefficients between adjacent lines of said transform;
- 5 ii. a bank of delay lines in a first group of $M/2$ alternating lines;
- iii. a second bank of butterfly lifting steps with unitary coefficients, and
- iv. a bank of pairs of butterfly lifting steps with coefficients of $1/2$ between $M/2 - 1$ pairs of said $M/2$ alternating lines;
- c. transmitting or storing the output coefficients of said $M \times M$ block coder;
- 10 d. receiving the output coefficients in a decoder; and
- e. processing the output coefficients in the decoder, comprising the steps of
 - i. processing the output coefficients through a cascade comprising a plurality of dyadic rational lifting transforms, each of said plurality of dyadic rational lifting transforms comprising
 - 15 a) a bank of pairs of butterfly lifting steps with coefficients of $1/2$ between said $M/2 - 1$ pairs of said $M/2$ alternating lines;
 - b) a first bank of pairs of butterfly lifting steps with unitary coefficients between adjacent lines of said transform;
 - c) a bank of delay lines in a second group of $M/2$ alternating lines;

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- d) a second bank of pairs of butterfly lifting steps with unitary coefficients between adjacent lines of said transform;
- e) a de-scaling bank; and
- f. processing the results of the preceding step in an inverse initial stage.

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15. *partial*
The apparatus of Claim 2, with any approximation of the
special constants in this patent filing.PT 12/13/98
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